

# The mating system of *Liatris helleri* (Asteraceae), a threatened plant species

MARY JO W. GODT\* & J. L. HAMRICK

*Departments of Botany and Genetics, University of Georgia, Athens, Georgia 30602, U.S.A.*

Multilocus outcrossing rates were estimated for seven populations of *Liatris helleri*, a rare insect-pollinated composite. The mean multilocus outcrossing rate was 0.97 (SE = 0.02). None of the populations examined had multilocus outcrossing rates that differed significantly from 1.00, suggesting that the species is self-incompatible. Seed set was insignificant for 770 bagged floral heads, lending further support for this view. A small but significant amount of biparental inbreeding was detected in three of the seven populations.

**Keywords:** conservation, endangered plant, *Liatris helleri*, mating system, outcrossing rate, self-incompatibility.

## Introduction

Appropriate management of rare plant species requires an understanding of their life-history characteristics. One of the life-history features critical to successful management is the mating system of the species (Karron, 1991). Knowledge of the mating system permits assessment of potential problems with the regeneration of natural and *ex situ* populations. For instance, small populations of self-incompatible plant species may not obtain sufficient pollen for maximum seed set if there is a small number of reproductive individuals or cross-compatible plants, or if there is variation in phenology among individuals (Les *et al.*, 1991; Whisler & Snow, 1992; Widén, 1993). In addition, self-compatible plants that typically outcross may experience higher rates of selfing and consequently higher inbreeding depression in small populations (Barrett & Kohn, 1991). In contrast, small population size may pose no particular recruitment threat to selfing plants unless necessary pollinator service is diminished. Population size enhancement, the introduction of plants carrying a variety of incompatibility alleles, hand-pollination and pollinator introductions could be utilized to ameliorate reproductive difficulties.

*Ex situ* conservation plans can also be enhanced by knowledge of the mating system. For instance, there is no need to maintain barriers to pollen flow among populations of selfing plants maintained off-site. In other cases, manipulation of gene flow (e.g.

assisted movement of pollen among self-incompatible plants) may be desirable.

## The study species

In this study we obtain quantitative estimates of the mating system of *Liatris helleri* (Porter) Porter, a rare herb of the south-eastern U.S. One objective was to examine whether inbreeding was correlated with population size. To this end, we collected *L. helleri* seeds from populations that ranged in size from approximately fifty flowering plants to over several hundred.

*Liatris helleri* (Heller's blazing star) is a rare high-elevation plant endemic to a small area of the Blue Ridge Mountains of North Carolina. A sun-loving perennial, *L. helleri* is found on open rocky outcrops, ledges and cliff faces and rarely, at wood edges, at high (1100 to 1800 m) elevations in generally shallow soils. The perennating organ is a corm-like rootstock that produces tufts of basal leaves. Flowering individuals send up several or more stems that reach 40 cm in height and are topped by a showy determinate spike of perfect, lavender to purple flowers. Seven to 10 florets form an *L. helleri* head (Massey *et al.*, 1983). Flowering occurs from late July to September (M.J.W.G., pers. obs.), with fruit-set occurring from September to October (Radford *et al.*, 1968). A variety of bees, butterflies, and moths visits the flowers (M.J.W.G., pers. obs.).

In 1989, *L. helleri* was given 'threatened' status under the United States Endangered Species Act. Various factors make the species vulnerable to

\*Correspondence.

extinction. One is the small number (seven) of extant populations (U. S. Fish and Wildlife Service, 1989). Demographic stochasticity and extremes of natural climatic conditions (e.g. severe drought) could easily lead to a decrease in the number of populations, many of which are small. In addition, the restricted range of the species makes it vulnerable to catastrophic events. Tangible threats to the species include (1) the recreational development of private sites that harbour populations, (2) succession, and (3) trampling by visitors and hikers who enjoy the scenic views obtained from the rock surfaces on which *L. helleri* grows (U. S. Fish & Wildlife Service, 1989).

## Materials and methods

### Collection and treatment of samples

*Liatris helleri* seeds were collected in autumn of 1992 from seven North Carolina populations. Sample sizes were restricted because of concern for the viability of populations. Populations (locations are not given because of the vulnerability of the species to collectors) were located within a 30 km radius. Seeds were sorted from chaff, marked by maternal family, planted shallowly in flats and stratified in a cold (2–4°C) room. After 3 months the flats were moved to a greenhouse. Seedlings began emerging after about 10 days, and whole plants were used in enzyme extractions that began 5 weeks after seedling emergence. After several additional weeks, plants reached sufficient size to permit nondestructive sampling, and plants were preserved for restoration. Enzymes were extracted from leaves of seedlings by crushing leaf tissue in a mortar and pestle with the addition of an extraction buffer (Mitton *et al.*, 1979). Extracts were absorbed onto chromatography paper wicks that were stored at –70°C until needed for electrophoresis.

### Electrophoresis and statistical analysis

Electrophoresis was performed using starch (Sigma) gels. Gels were stained for seven enzyme systems to resolve nine polymorphic allozyme loci: leucine aminopeptidase (*Lap*, EC 3.4.11.-), phosphoglucosmutase (*Pgm-1* and *-2*, EC 5.4.2.2), diaphorase (*Dia-1*, EC 1.8.1.4), menadione reductase (*Mnr-2*, EC 1.6.99.2), fluorescent esterase (*Fe-2*, EC 3.1.1.1), phosphogluco-isomerase (*Pgi-2* and *-3*, EC 5.3.1.9), and triose phosphate isomerase (*Tpi-1*, EC 5.3.1.1). The following buffer systems of Soltis *et al.* (1983) were used in the analyses: System 10 (for LAP and

PGM); System 7 (for DIA and MNR); and a modified System 8 (for FE, PGI and TPI). Stain recipes were from Soltis *et al.* (1983), except for DIA and MNR which were from Cheliak & Pitel (1984). Subsets of the nine loci (Table 1) were used to estimate outcrossing rates in different populations, because not all loci were polymorphic in every population.

Single locus ( $t_s$ ) and multilocus ( $t_m$ ) outcrossing estimates, pollen allele frequencies, and maternal inbreeding coefficients ( $F$  values) were estimated by the computer program of Ritland & Jain (1981) which is based on the mixed-mating model of Brown & Allard (1970). Assumptions of the mixed-mating model are that each mating results either from a random mating event or a selfing event; that selection has not occurred between the time of fertilization and the time of assay; that the likelihood of an outcross event is independent of maternal genotype; and that maternal individuals obtain equivalent samples of outcross pollen (Clegg, 1980). An additional assumption of the multilocus estimation procedures is that the study loci are unlinked (Shaw *et al.*, 1981).

Maternal genotypes were inferred from progeny arrays (by the method of Brown & Allard (1970)), because leaves of maternal individuals were in poor condition at the time of seed harvest. For those loci that had more than three alleles in a population the lowest-frequency alleles were pooled for statistical analyses because Ritland's mating system program handles a maximum of three alleles at a locus. Standard errors for the outcrossing estimates were based on 200 bootstraps.

For population estimates of outcrossing rates, an average of 12 individuals per family was assayed. In total, 1104 individuals representing 95 families were analysed. In addition, 48 individuals were analysed

**Table 1** The number of alleles found at each locus analysed for the mating system of *Liatris helleri*

Locus	Population						
	BH	CR	GF	RR	SH	TR	YO
<i>Dia-1</i>	2	2	2	2	2	2	2
<i>Fe-2</i>	2	2	2	2	2	3	2
<i>Lap</i>	2	3	3	3	4	3	2
<i>Mnr-2</i>	5	5	4	5	5	4	6
<i>Pgi-2</i>	4	2	2	2	2	2	2
<i>Pgi-3</i>	1	4	1	1	1	5	1
<i>Pgm-1</i>	2	2	2	3	3	2	2
<i>Pgm-2</i>	1	2	1	2	2	4	2
<i>Tpi-1</i>	2	3	3	2	2	4	2

for each of 11 families and 13 families in the GF and TF populations, respectively. To test for differences in pollen allele frequencies among families, the progeny of maternal individuals with the same genotype were examined using contingency chi-square tests. For homozygous mothers, the numbers of heterozygous vs. homozygous progeny were compared. At diallelic loci an even segregation ratio was assumed for heterozygous mothers, and pollen allele numbers were calculated by subtracting the maternal alleles donated to the progeny. The numbers of pollen alleles in each class were then compared across families. Not all loci could be tested because the distribution of genotypes for some loci did not conform to the number required for valid chi-square tests (i.e. genotype 'cells' should have expected values of 5 or more).

The expected inbreeding coefficient at equilibrium ( $F_e$ ) was calculated (Fyfe & Bailey, 1951) from the multilocus outcrossing rates by the equation  $F_e = (1 - t_m)/(1 + t_m)$ . The expected equilibrium inbreeding coefficient and the observed inbreeding coefficient should be equal if the assumptions of Hardy-Weinberg are met, and if the mating system is the sole factor determining genotype frequencies.

To test the ability of plants to self, flowering stalks of 30 individuals were bagged in the greenhouse with either white paper bags (18 individuals) or bags constructed of very fine netting material (12 individuals). After flower stalks senesced, inflorescences were removed and the numbers of bagged heads and seeds were counted.

## Results

*Liatris helleri* was found to be highly outcrossed, with a mean multilocus outcrossing estimate of  $0.97 \pm 0.02$  (Table 2). The multilocus outcrossing

rate did not differ significantly from unity for any population. The mean single-locus outcrossing estimate (mean  $t_s = 0.87 \pm 0.03$ ) was somewhat lower than the multilocus estimate, and ranged from 0.78 to 1.00 for the different populations. Differences between multilocus and mean single-locus outcrossing rates for individual populations provide a measure of biparental inbreeding (Brown, 1989). We found significant differences between  $t_m$  and  $t_s$  for three (CR, RR and TR) of the seven populations examined (Table 2).

Significant differences were found between ovule allele frequencies and frequencies of successful pollen alleles at a number of loci in several populations (Table 3), indicating violations of the mixed-mating model assumptions. To examine the effect of these violations on outcrossing rate estimates in populations BH and RR, two analyses were performed in which the loci with the greatest deviations were omitted. When *Mnr-2* was omitted from the analysis for RR, the multilocus outcrossing rate decreased from 0.951 (SE = 0.037) to 0.949 (SE = 0.050), while the mean single-locus estimate increased from 0.785 (SE = 0.060) to 0.818 (SE = 0.074). For population BH, two loci (*Lap* and *Tpi-1*) violated model assumptions. When these were omitted from the analysis, the multilocus outcrossing rate decreased from 0.880 (SE = 0.089) to 0.848 (SE = 0.137), and the mean single-locus estimate fell from 0.844 (SE = 0.094) to 0.833 (SE = 0.118). Since outcrossing estimates did not change significantly when loci that violated assumptions of the mixed-mating model were eliminated, all polymorphic loci were utilized in the estimation of outcrossing rates (Table 1).

A total of nineteen tests were conducted to examine whether pollen allele frequencies were similar across maternal individuals within populations. Eight

**Table 2** Mating system estimates\* and sampling parameters for seven *Liatris helleri* populations

Population	No. of families	Total no. of progeny	No. of loci used	$t_m$ (SE)	$t_s$ (SE)	$t_m - t_s$ (SE)
BH	7	78	7	0.88 (0.09)	0.84 (0.09)	0.04 (0.06)
CR	17	200	9	0.97 (0.03)	0.78 (0.04)	0.19 (0.03)
GF	21	252	7	0.95 (0.03)	0.90 (0.04)	0.05 (0.03)
RR	10	119	8	0.95 (0.04)	0.79 (0.06)	0.16 (0.04)
SH	7	84	8	1.01 (0.28)	0.93 (0.07)	0.08 (0.25)
TR	21	252	9	0.96 (0.03)	0.85 (0.05)	0.11 (0.03)
YO	12	119	8	1.04 (0.14)	1.00 (0.11)	0.04 (0.06)
Mean				0.97 (0.02)	0.87 (0.03)	0.10 (0.02)

\* $t_m$  is the multilocus outcrossing rate,  $t_s$  is the mean single-locus outcrossing rate and SE is the standard error.

**Table 3** Loci with significant differences between ovule and pollen allele frequencies in *Liatris helleri* populations

Population	Locus	Source	Allele frequency		
			1	2	3
BH	<i>Lap</i>	Ovule	0.071	0.929	
		Pollen	0.190	0.810	
	<i>Tpi-1</i>	Ovule	0.857	0.143	
		Pollen	0.634	0.366	
CR	<i>Dia-1</i>	Ovule	0.735	0.265	
		Pollen	0.405	0.595	
	<i>Lap</i>	Ovule	0.206	0.676	0.118
		Pollen	0.396	0.563	0.041
	<i>Mnr-2</i>	Ovule	0.206	0.500	0.294
		Pollen	0.252	0.379	0.369
	<i>Pgi-2</i>	Ovule	0.471	0.529	
		Pollen	0.472	0.528	
	<i>Pgm-1</i>	Ovule	0.441	0.559	
		Pollen	0.391	0.609	
GF	<i>Mnr-2</i>	Ovule	0.310	0.143	0.548
		Pollen	0.320	0.226	0.454
	<i>Pgi-2</i>	Ovule	0.381	0.619	
		Pollen	0.439	0.561	
RR	<i>Fe-2</i>	Ovule	0.250	0.750	
		Pollen	0.408	0.592	
	<i>Mnr-2</i>	Ovule	0.400	0.350	0.250
		Pollen	0.292	0.288	0.420
	<i>Pgi-2</i>	Ovule	0.200	0.800	
		Pollen	0.351	0.649	
	<i>Pgm-2</i>	Ovule	0.950	0.050	
		Pollen	0.934	0.066	
	<i>Tpi-1</i>	Ovule	0.550	0.450	
		Pollen	0.568	0.432	
TR	<i>Mnr-2</i>	Ovule	0.667	0.214	0.119
		Pollen	0.707	0.215	0.078
	<i>Pgi-3</i>	Ovule	0.381	0.310	0.310
		Pollen	0.264	0.450	0.286
	<i>Pgm-1</i>	Ovule	0.667	0.333	
		Pollen	0.643	0.357	
	<i>Pgm-2</i>	Ovule	0.000	0.762	0.238
		Pollen	0.001	0.773	0.227
YO	<i>Fe-2</i>	Ovule	0.958	0.042	
		Pollen	0.866	0.134	
	<i>Pgm-1</i>	Ovule	0.958	0.042	
		Pollen	0.907	0.093	

of these tests were significant ( $P < 0.05$ ), indicating that the pollen that had been successful in fertilizing different plants varied significantly in allele frequency among maternal plants.

Inbreeding coefficients for maternal individuals ranged from  $-0.300$  in YO to  $0.225$  in SH, with an overall mean of  $-0.096$  (Table 4). Four of the seven inbreeding coefficients differed significantly from

zero, with one being positive (SH) and three negative (RR, TR and YO). The equilibrium inbreeding coefficients were low, with a mean of  $0.021$ .

For the 30 individuals with bagged flowers, we examined 770 heads for seed set. With the exception of 10 seeds produced by one individual, no seeds were produced, indicating that the species does not self, at least in the absence of insect vectors.



**Table 4** Mean observed fixation index ( $F_{IS}$ ) and the equilibrium fixation index ( $F_e$ ) for populations of *Liatris helleri*

Population	$F_{IS}$ (SE)	$F_e$
BH	-0.266 (0.104)	0.064
CR	0.051 (0.089)	0.015
GF	0.095 (0.088)	0.026
RR	-0.262 (0.099)	0.026
SH	0.225 (0.095)	0.000
TR	-0.213 (0.074)	0.000
YO	-0.300 (0.002)	0.015
Mean	-0.096 (0.081)	0.021

## Discussion

Multilocus outcrossing rates for populations of *L. helleri* did not differ significantly from one, suggesting that the species is self-incompatible. The results of greenhouse tests supported this conclusion. Only one of 30 plants with a total of 770 bagged floral heads set a few seeds. The seeds produced by this individual may have resulted from a poor seal on the pollen exclusion bag or a leaky self-incompatibility system. Three other species of *Liatris* are reported to be obligate outcrossers (Cruise, 1964), as indicated by low levels of seed set in bagged inflorescences.

Significant differences were found between pollen and ovule allele frequencies at certain loci in six of the seven populations surveyed. Nonrandom mating, or gene flow into the populations could contribute to these differences. Pollinators can be preferentially attracted to plants with large floral displays, with the result that such plants may have higher male fertilities (Broyles & Wyatt, 1990). Thus, although ovule allele frequencies are based on all reproductive individuals collected, pollen allele frequencies represent a sample of the successful pollen and include any biases that may occur in fertility. For *L. helleri*, the number of flowering stalks per plant and inflorescence size vary widely in natural populations and these factors coupled with pollinator foraging behaviour may have contributed to differences between pollen and ovule allele frequencies.

It is also possible that the maternal individuals sampled were not a representative sample of reproductive individuals in the population. A larger number of *L. helleri* plants flowered than set seed. The difference in the numbers of individuals setting seed and flowering resulted from in large part to broken flowering stalks.

Low levels of biparental inbreeding (mating

between related individuals) were evident from the significant  $t_m - t_s$  values recorded in three of the populations examined. Localized seed dispersal, coupled with local pollen transfer, can lead to the development of population subdivision and biparental inbreeding. Schaal & Levin (1978) found evidence for population subdivision in a related species, *Liatris cylindracea*, and attributed it to consanguineous matings. Bees mediate most pollen dispersal in *L. cylindracea*, and travel predominantly between near-neighbours (Levin & Kerster, 1969; Schaal, 1975). These neighbours are likely to be related, because mean seed dispersal distance for *L. cylindracea* was estimated as 1.61 m in open surroundings, with a modal distance of 0.75 m (Schaal & Levin, 1978). For *L. helleri*, the majority of pollinator movements is also likely to be between closely spaced individuals. However, parameters of *L. helleri* seed dispersal are more difficult to assess. Seeds of *L. helleri* are wind-dispersed, and high winds are common in the mountainous habitat of *L. helleri*, particularly during the autumn when seeds are ripening. The distance that *L. helleri* seeds typically travel, however, before being intercepted by intervening vegetation is unknown.

We found no evidence that biparental inbreeding was associated with the number of flowering plants in a population. Significant levels of inbreeding were not observed in the smallest populations (YO, SH and BR). Because pollinator behaviour is likely to be similar across populations, this suggests that stochastic seed dispersal and establishment may lead to less population structure in some populations. Suitable open habitat is limited in many populations, adding elements of chance to establishment and recruitment.

Overall, equilibrium inbreeding coefficients were low, as expected for an outcrossing species. If the mating system is the sole determinant of genotypic proportions, the equilibrium inbreeding coefficient and the inbreeding coefficient of the adult plants should be similar. For three of the seven populations we found no significant differences. However, in populations RR, TR and YO an excess of heterozygotes was observed in the adult generation, while a deficit of heterozygotes was observed in population SH.

## Conservation implications

It is likely that *L. helleri* has a multiallelic sporophytic incompatibility system, which is typical of the Asteraceae (Richards, 1986). In this self-incompatibility system, populations consist of many mating

types that differ in 'S' alleles at the self-incompatibility locus. The ability of the pollen grain to effect fertilization is determined by the similarity between the genotype of the pollen donor and the plant receiving pollen, rather than between the genotype of the pollen grain and the target plant. Frequency-dependent selection favours rare S alleles as individuals carrying such alleles are initially compatible with a large number of plants. Theoretically, most populations should contain several alleles in roughly even frequencies. Loss of S alleles during a population bottleneck or during a founding event should decrease the number of compatible mating types, and might lead to decreased reproduction (this can also result from stochastic events in small populations). In the extreme case, all plants could have the same mating type, in which case the population would be effectively sterile. This scenario was documented for a remnant inland population of the lakeside daisy (*Hymenoxys acaulis* var. *glabra*), a Great Lake endemic (DeMauro, 1993). A low number of compatible mating types in *L. helleri* populations might explain the large proportion of achenes that were observed to have aborted at the time of collection (M.J.W.G., pers. obs.). Incompatible pollen (either self or outcross) may swamp the stigma or plug the style before outcrossed pollen from a compatible mating type arrives. The small number of reproductive individuals in some *Liatris* populations suggests that this may not be an unlikely event. However, cross-incompatibility can occur among plants even within large populations, suggesting that compatible mating types may be locally rare (DeMauro, 1993).

Because *L. helleri* is self-incompatible, individuals isolated from the main body of a population may be pollen-limited. However, because *L. helleri* racemes bloom sequentially from top to bottom over a fairly extended period, and because different flowering stalks on the same plant can have different phenologies, opportunities for obtaining outcross pollen are enhanced.

It is evident from the results of the present study that future management and conservation plans for *L. helleri* must take into account its mating system. Restoration efforts are likely to falter or fail if insufficient numbers of cross-compatible mating types are not maintained in populations. Likewise, *ex situ* conservation and propagation of the species will require a variety of cross-compatible genotypes.

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